### Neural Networks: Old and New

Ju Sun

Computer Science & Engineering University of Minnesota, Twin Cities

January 29, 2020

#### Logistics

 Another great reference: Dive into Deep Learning by Aston Zhang and Zachary C. Lipton and Mu Li and Alexander J. Smola. Livebook online: https://d2l.ai/ (comprehensive coverage of recent developments and detailed implementations based on NumPy)



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- Waiting list

Start from neurons

Shallow to deep neural networks

A brief history of Al

Suggested reading



A cartoon drawing of a biological neuron (left) and its mathematical model (right).

Credit: Stanford CS231N

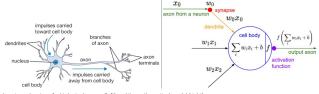


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Biologically ...

- Each neuron receives signals from its dendrites

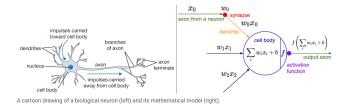


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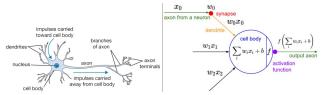
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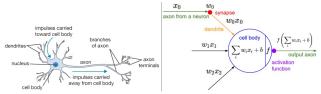
Biologically ...

- Each neuron receives signals from its dendrites
- Each neuron outputs signals via its single axon
- The axon branches out and connects via synapese to dendrites of other neurons



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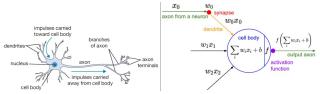


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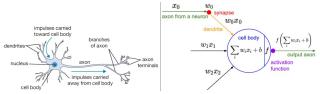


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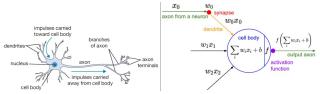


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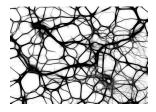
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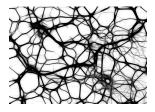
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- The neuron fires only when the combined signal is above a certain threshold:  $\sum_i w_i x_i + b$
- Fire rate is modeled by an **activation function** f, i.e., outputting  $f(\sum_i w_i x_i + b)$

Brain neural networks



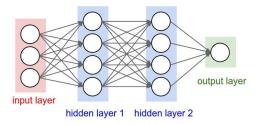
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#### Brain neural networks

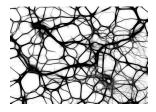


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#### Artificial neural networks



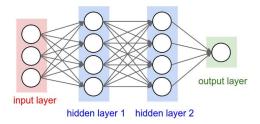
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#### Why called artificial?

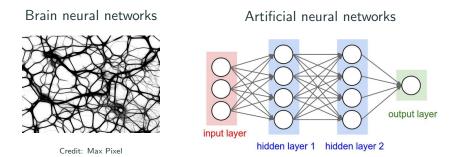
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# Brain neural networks Artificial neural networks

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- (Over-)simplification on neural level
- (Over-)simplification on connection level



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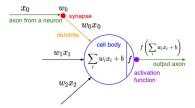
In this course, neural networks are always artificial.

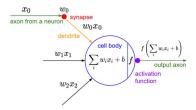
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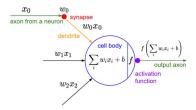
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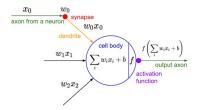


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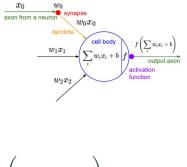
We shall use  $\sigma$  instead of f henceforth.



#### Examples of activation function $\boldsymbol{\sigma}$

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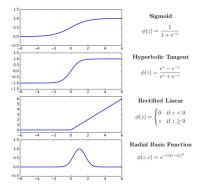
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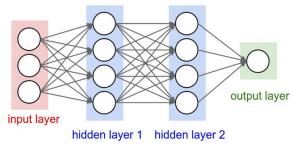
#### Examples of activation function $\sigma$



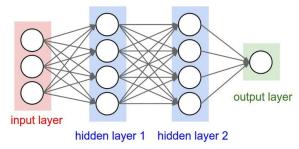
Credit: [Hughes and Correll, 2016]

One neuron:  $\sigma (\boldsymbol{w}^{\mathsf{T}} \boldsymbol{x} + b)$ 

One neuron:  $\sigma (w^{\intercal}x + b)$ Neural networks (NN): structured organization of artificial neurons

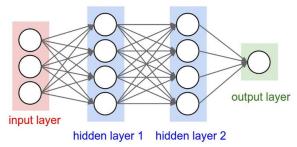


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One neuron:  $\sigma (w^{T}x + b)$ Neural networks (NN): **structured** organization of artificial neurons



w's and b's are unknown and need to be learned Many models in machine learning **are** neural networks

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 $\ldots$  known as **empirical risk minimization** (ERM) framework in learning theory

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#### Supervised Learning from NN viewpoint

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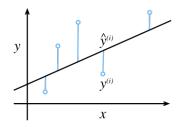
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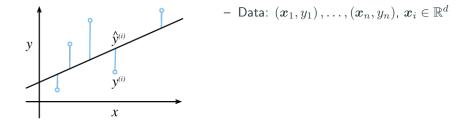
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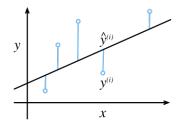
$$\min_{\boldsymbol{w}'s, \boldsymbol{b}'s} \frac{1}{n} \sum_{i=1}^{n} \ell \left[ \boldsymbol{y}_i, \left\{ \mathsf{NN}\left( \boldsymbol{w}_1, \dots, \boldsymbol{w}_k, b_1, \dots, b_k \right) \right\} (\boldsymbol{x}_i) \right]$$



Credit: D2L



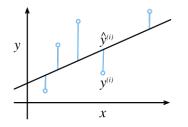
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– Data:  $(oldsymbol{x}_1, y_1), \ldots, (oldsymbol{x}_n, y_n)$ ,  $oldsymbol{x}_i \in \mathbb{R}^d$ 

- Model: 
$$y_i \approx \boldsymbol{w}^{\mathsf{T}} \boldsymbol{x}_i + b$$

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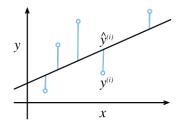


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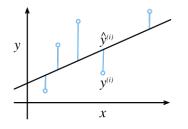


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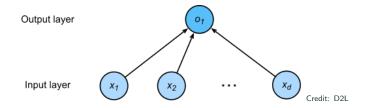
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 $\sigma$  is the identity function



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(1928-1971)



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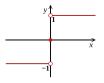
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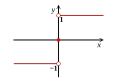




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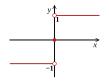
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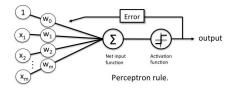
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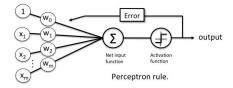
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Perceptron is a single artificial neuron for binary classification

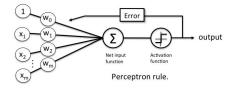


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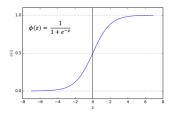
dominated early AI (50's - 70's)

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Logistic regression is similar but with sigmod activiation



- Data:  $(x_1, y_1), \ldots, (x_n, y_n)$ ,  $x_i \in \mathbb{R}^d$ ,  $y_i \in \{L_1, \ldots, L_p\}$ , i.e., multiclass classification problem

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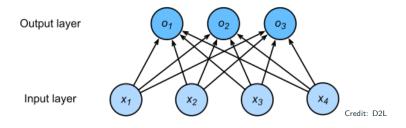
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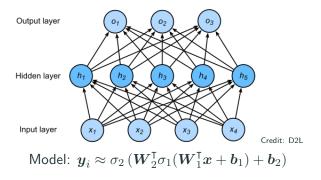
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- Optimization ...

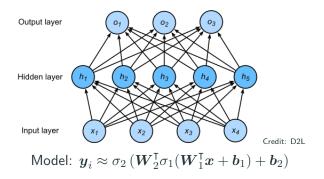
#### ... for multiclass classification



### Multilayer perceptrons

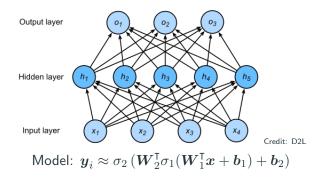


## **Multilayer perceptrons**



#### Also called feedforward networks

## Multilayer perceptrons



#### Also called feedforward networks

Modern NNs: many hidden layers (deep), refined connection structure and/or activations

# They're all (shallow) NNs

- Linear regression
- Perception and Logistic regression
- Softmax regression
- Multilayer perceptron (feedforward NNs)

- Linear regression
- Perception and Logistic regression
- Softmax regression
- Multilayer perceptron (feedforward NNs)
- Support vector machines (SVM)
- PCA (autoencoder)
- Matrix factorization

see, e.g., Chapter 2 of [Aggarwal, 2018].

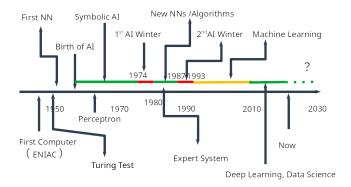
Start from neurons

Shallow to deep neural networks

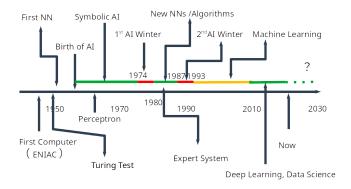
A brief history of AI

Suggested reading

Birth of AI

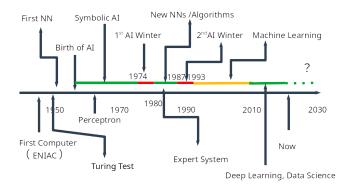


Birth of AI

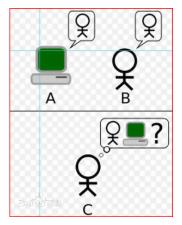


- Crucial precursors: first computer, Turing test

Birth of AI



- Crucial precursors: first computer, Turing test
- 1956: Dartmouth Artificial Intelligence Summer Research
   Project Birth of Al

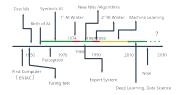


Turing Test

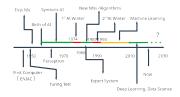


Alan Turing (1912-1954)

## First golden age

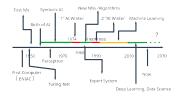


## First golden age

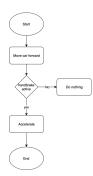


Symbolic AI: based on rules and logic

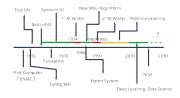
## First golden age



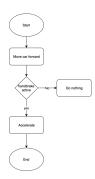
Symbolic AI: based on rules and logic



## First golden age



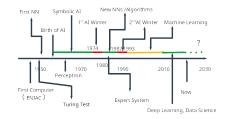
Symbolic AI: based on rules and logic



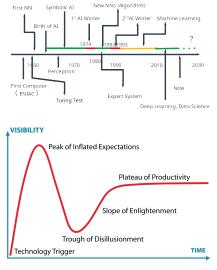


rules for recognizing dogs?

## **First AI winter**

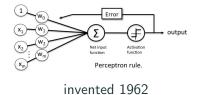


## First AI winter

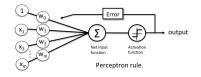


Gartner hype cycle

## Perceptron



## Perceptron



invented 1962



written in 1969, end of Perceptron era



Marvin Minsky (1927–2016)

## Birth of computer vision

MASSACHUSETTS INSTITUTE OF TECHNOLOGY PROJECT MAC

Artificial Intelligence Group Vision Memo. No. 100. July 7, 1966

#### THE SUMMER VISION PROJECT

Seymour Papert

The summer vision project is an attempt to use our summer vorkers effectively in the construction of a significant part of a visual system. The particular task was chosen partible because it can be segmented into sub-problems which will allow individuals to work independently and yet participate in the construction of a system complex enough to be a real lumbark in the development of "mattern recognized."

1966

# VISION

Convrighted Material



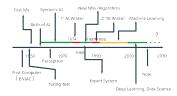
#### **David Marr**

FOREWORD BY Shimon Ullman AFTERWORD BY Tomaso Poggio

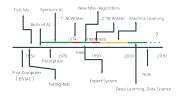
Copyrighted Material

### around 1980

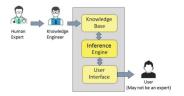
## Second golden age



## Second golden age



expert system



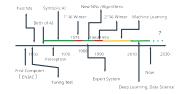


Can we build comprehensive knowledge bases and know all rules?

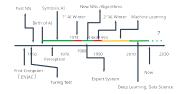
## Key ingredients of DL have been in place for 25-30 years:

Landmark	Emblem	Epoch
Neocognitron	Fukushima	1980
CNN	Le Cun	mid 1980s'
Backprop	Hinton	mid 1980's
SGD	Le Cun, Bengio etc	mid 1990's
Various	Schmidhuber	mid 1980's
CTF	DARPA etc	mid 1980's

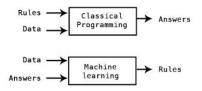
## After 2nd AI winter



## After 2nd Al winter



Machine learning takes over ...



Starting 1990's

Support vector machines (SVM) Adaboost Decision trees and random forests Deep learning Start from neurons

Shallow to deep neural networks

A brief history of Al

Suggested reading

- Chap 2, Neural Networks and Deep Learning.
- Chap 3-4, Dive into Deep Learning.
- Chap 1, Deep Learning with Python.

- [Aggarwal, 2018] Aggarwal, C. C. (2018). Neural Networks and Deep Learning. Springer International Publishing.
- [Hughes and Correll, 2016] Hughes, D. and Correll, N. (2016). Distributed machine learning in materials that couple sensing, actuation, computation and communication. *arXiv:1606.03508*.